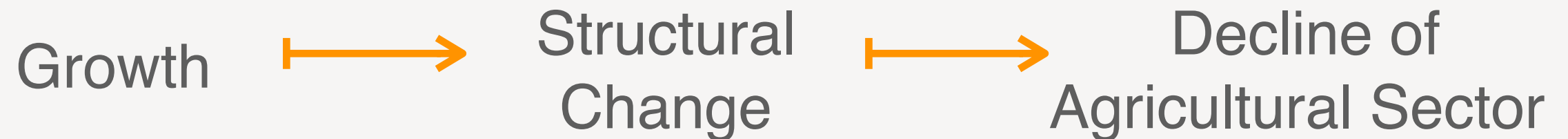


Spatial Structural Change

Fabian Eckert (UCSD) and Michael Peters (Yale)

September 2022

Spatial Structural Change



Question: Systematic spatial bias?

- Are rural locations hurt by declining demand?
- Does industrialization offer new opportunities for rural labor markets?

This paper: The US experience from 1880-1920

- Empirical finding: growth was **rural** biased
 - Spatial convergence
- Novel theory of **spatial** structural change
 - Macro model of structural change + Quantitative spatial model
 - **Catch-up growth** through technology diffusion
- Quantitative analysis
 - Important role for catch-up growth
 - Main beneficiaries: rural locations

Literature

- **Structural Change**

Herrendorf et al. (2014), Kongsamut et al. (2001), Gollin et al. (2002), Comin et al. (2017), Boppart (2014), Ngai and Pissarides (2007), Acemoglu and Guerrieri (2008), Alvarez-Cuadrado et al. (2017), Caselli and Coleman II (2001), Porzio et al. (2020))

- **Quantitative Geography**

Allen, Arkolakis (2014), Redding, Rossi-Hansberg (2017), Desmet, Nagy, Rossi-Hansberg (2018), Allen, Donaldson (2022), Peters (2021)

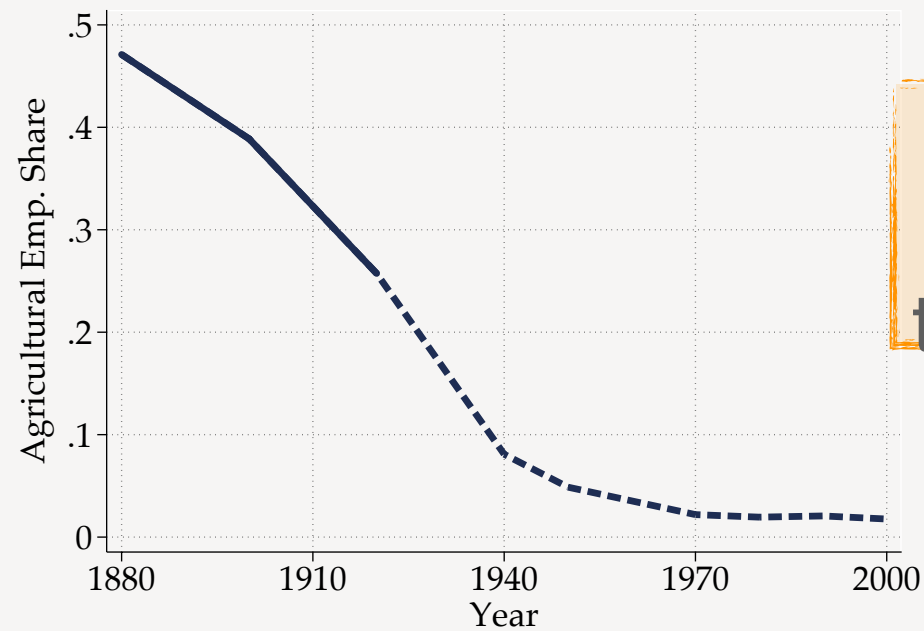
- **Spatial Structural Change**

Caselli. Coleman (2001), Nagy (2021), Budí-Ors, Pijoan-Mas (2022), Desmet and Rossi-Hansberg (2014), Fan et al. (2021), Eckert et al. (2022)

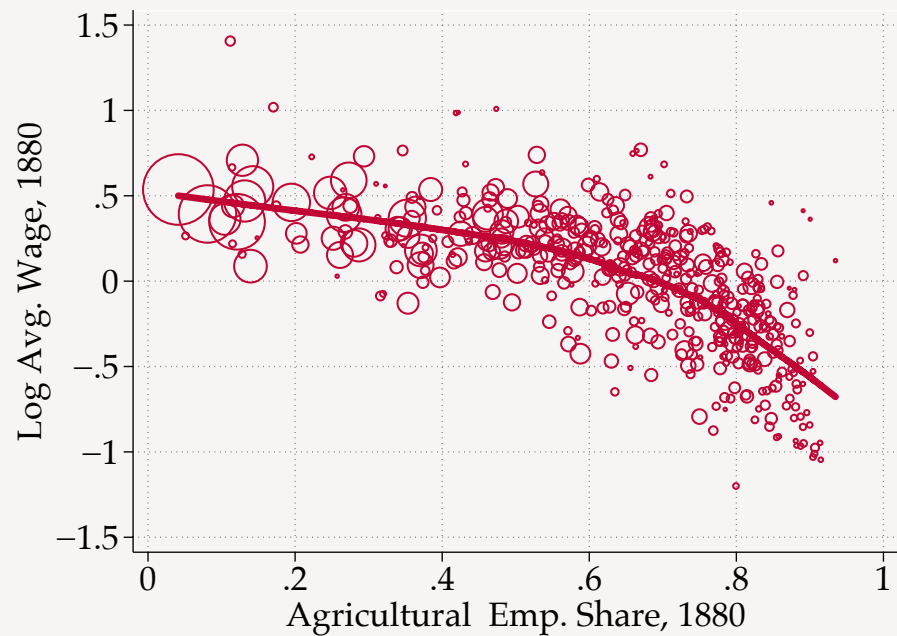
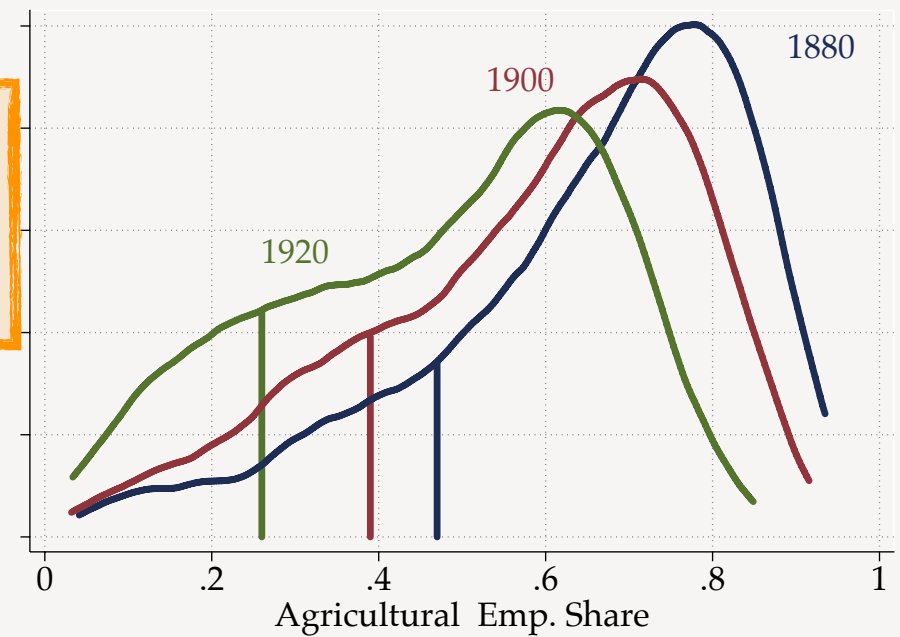
- **Convergence**

Barro and Sala-i Martin (1992), Acemoglu et al. (2006), Desmet, Rossi-Hansberg (2009)

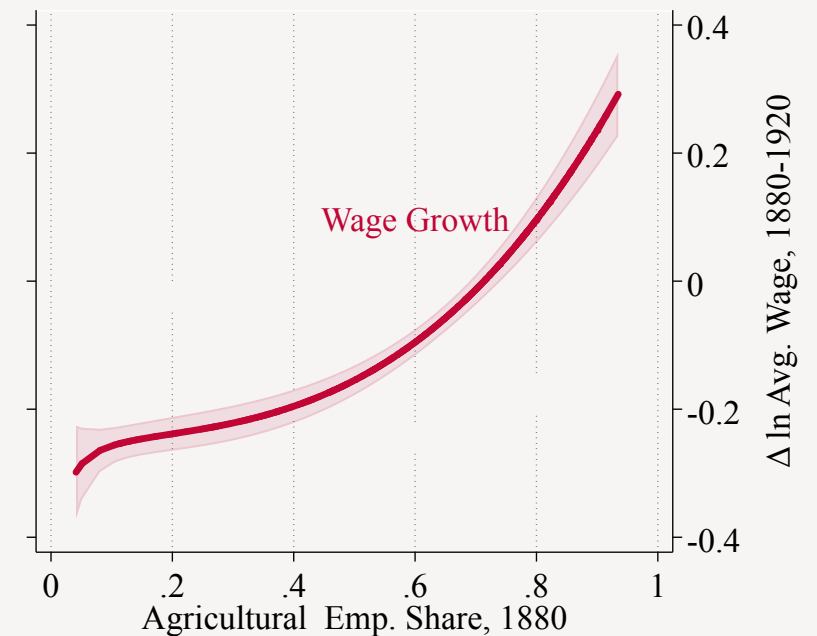
Spatial Structural Change in the US



Local
structural
transformation



Rural catch-up



Today

- Theory
- Mechanism
- Estimation / Calibration
- Quantification: Importance of Rural Catch-Up

Today

- Theory
- Mechanism
- Estimation / Calibration
- Quantification: Importance of Rural Catch-Up

Technology

- R locations, $r = 1, \dots, R$
- Two sectors $s = A, M$ in each location
 - Agriculture: Homogeneous good

$$Y_{rAt} = Z_{rAt} H_{rAt}^{1-\alpha} T_{rt}^{\alpha}$$

- Non-agriculture: Differentiated varieties ω

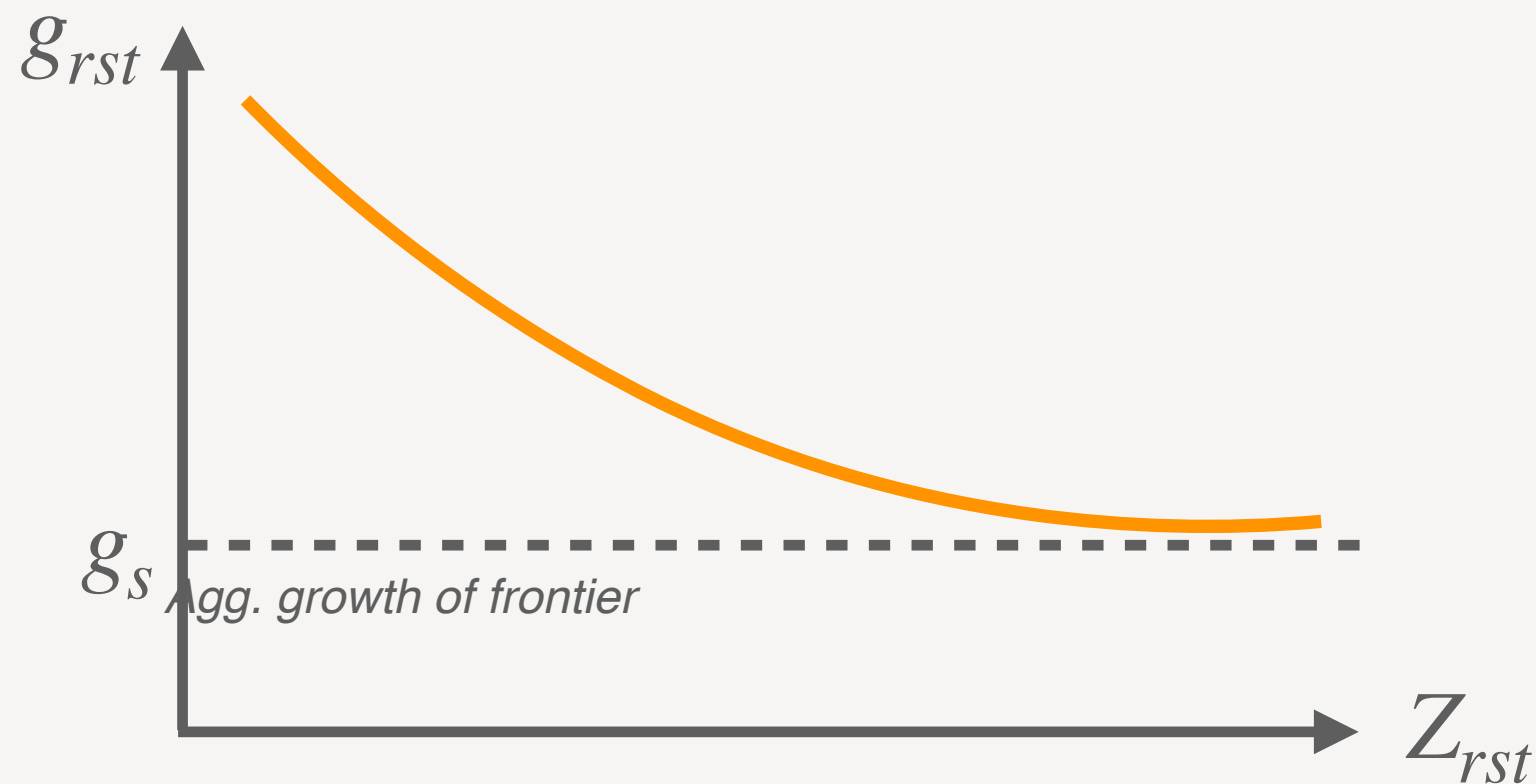
$$y_{rt}(\omega) = Z_{rMt} h_{rMt}(\omega) \quad \text{and} \quad Y_{rM} = \left(\sum_{r=1}^R \int_{\omega}^{N_{rt}} y_{rt}(\omega)^{\frac{\sigma-1}{\sigma}} d\omega \right)^{\frac{\sigma}{\sigma-1}}$$

Monopolistic competition; free entry at cost $f_E w_{rMt}$

The Spatial Productivity Ladder: Catch-up growth

- In each sector: technological **frontier** $\bar{Z}_{st}$; constant growth g_s
- **Local** productivity growth depends on **distance to frontier**

$$g_{rst} \equiv d \ln Z_{rst} = g_s + \lambda_s \times \ln (\bar{Z}_{st}/Z_{rst})$$

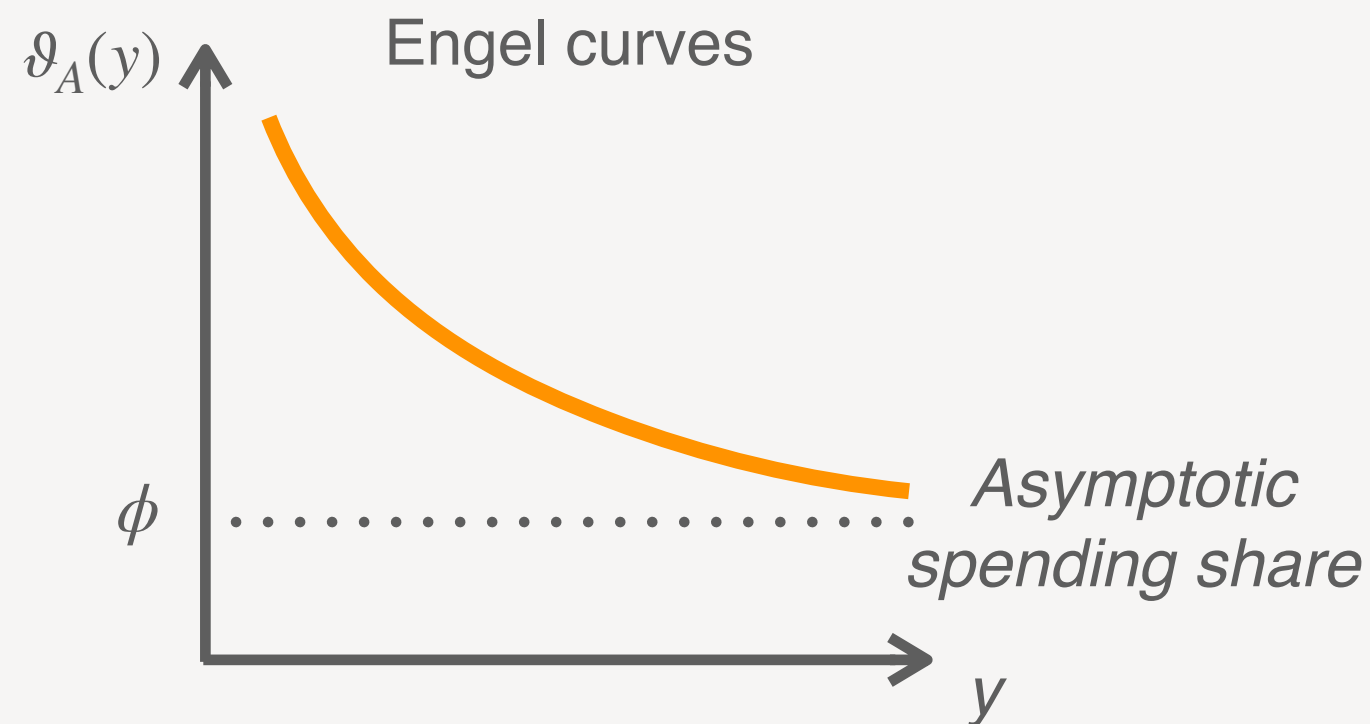


Note: Catch-up in **rural** regions is **not** hardwired

Preferences

- Nonhomothetic preferences; *PIGL* class [Boppart 2014]

$$\begin{array}{ccc} \text{Indirect utility} & & \text{Agricult. expenditure share} \\ V = \frac{1}{\eta} \left(\frac{y}{P_{rA}^\phi P_{rNA}^{1-\phi}} \right)^\eta - \nu \ln \left(\frac{P_{rA}}{P_{rNA}} \right) & \longrightarrow & \vartheta_A(y) = \phi + \nu \left(\frac{y}{P_{rA}^\phi P_{rNA}^{1-\phi}} \right)^{-\eta} \end{array}$$



- Main appeal of PIGL: Aggregation with heterogeneity

Aggregation

EOS

Closing the Model

▸ Sectoral labor supply:

- Idiosyncratic Fréchet productivity for each sector
- ζ = elasticity of substitution of workers across sectors

$$H_{rs} = \Gamma_{\zeta} L_r (w_{rs}/\bar{w}_r)^{\zeta-1}$$

▸ Spatial labor supply:

- Moving costs μ_{jr} and Fréchet taste draw with shape ϵ ; amenities

$$\mathcal{B}_{rt} = B_r L_{rt}^{-\rho}$$

- Exog. population shocks n_{rt} : intl. migration & fertility
- Slow-moving population dynamics

$$L_{rt} = \sum_j m_{jrt} n_{jt-1} L_{jt-1}$$

where

$$m_{krt} = \frac{(\mu_{kr} \mathcal{V}_{rt} \mathcal{B}_{rt})^{\epsilon}}{\sum_j (\mu_{rj} \mathcal{V}_{jt} \mathcal{B}_{jt})^{\epsilon}}$$

$\mathcal{V}_{rt} = \int V_{rt}(y) dF_{rt}(y)$

Static equilibrium: Characterization

▸ Two useful endogenous objects:

- **Manufacturing** market access: $\mathcal{D}_{rt} \equiv \sum \tau_{rj}^{1-\sigma} P_{jMt}^{\sigma-1} \left(1 - \vartheta_{jAt}\right) \Gamma_{\zeta} L_{jt} \bar{w}_j$
- **Agricultural** population density: $\ell_{rt} \equiv L_{rt}/T_{rt}$

Proposition: Let $\mathcal{F}_{rMt} \equiv \mathcal{D}_{rt}^{\frac{1}{\sigma}} Z_{rMt}^{\frac{\sigma-1}{\sigma}}$ and $\mathcal{F}_{rAt} \equiv Z_{rAt} \ell_{rt}^{-\alpha}$. Then

$$w_{rMt} = \mathcal{F}_{rMt} \quad ; \quad \left(\left(\frac{\mathcal{F}_{rMt}}{w_{rAt}} \right)^{\zeta} + 1 \right)^{\frac{\zeta-1}{\zeta}} \left(\frac{\mathcal{F}_{rAt}}{w_{rAt}} \right)^{\frac{1}{\alpha}} = 1 \quad ; \quad \frac{s_{rA}^{1+(\zeta-1)\alpha}}{1-s_{rA}} = \left(\frac{\mathcal{F}_{rAt}}{\mathcal{F}_{rMt}} \right)^{\zeta}$$

Today

- Theory
- Mechanism
- Estimation / Calibration
- Quantification: Importance of Rural Catch-Up

Drivers of Spatial Structural Change

- Determinants of local **wage growth** $d \ln \bar{w}_{rt}$ and local **industrialization** ds_{rAt}

Local income growth:

$$d \ln \bar{w}_{rt} = \underbrace{\phi(s_{rA})}_{\text{Exposure ("Bartik")}} \underbrace{d \ln \mathcal{F}_{rMt}}_{\text{Shock}} + \left(1 - \underbrace{\phi(s_{rA})}_{\text{Exposure ("Bartik")}}\right) \underbrace{d \ln \mathcal{F}_{rAt}}_{\text{Shock}}$$

Local industrialization:

$$ds_{rAt} = \underbrace{\psi(s_{rA})}_{\text{Exposure ("Bartik")}} \left(\underbrace{d \ln \mathcal{F}_{rMt}}_{\text{Shock}} - \underbrace{d \ln \mathcal{F}_{rAt}}_{\text{Shock}} \right)$$

$$\gamma \equiv \alpha(\zeta - 1)$$

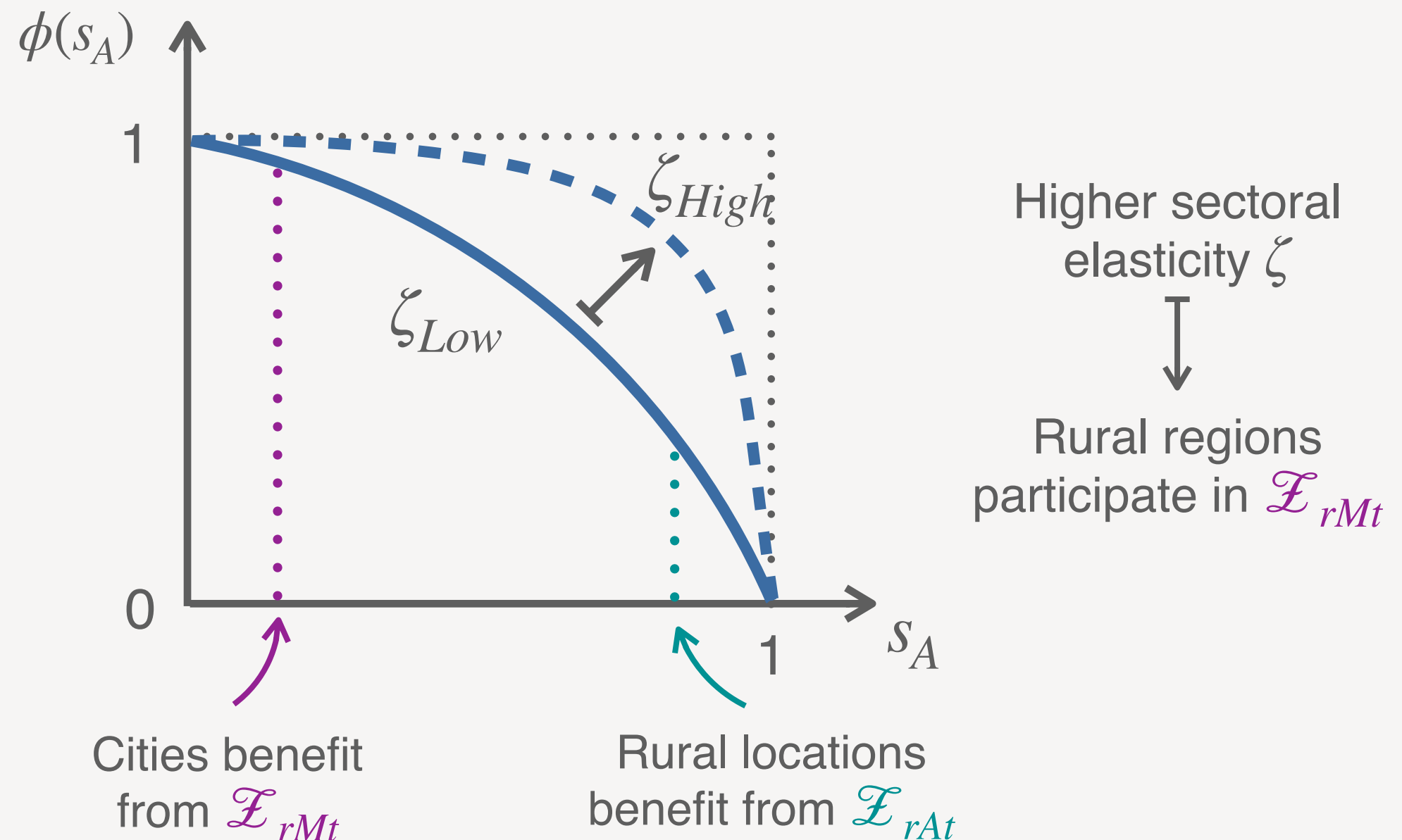
$$\phi_{NA}(s_{rA}) = \frac{(\gamma + 1)(1 - s_{rA})}{\gamma(1 - s_{rA}) + 1}$$

$\uparrow$
 s_{rA} = sufficient statistic
 $\downarrow$

$$\psi(s_{rA}) = - \frac{s_{rA}(1 - s_{rA})\zeta}{\gamma(1 - s_{rA}) + 1}$$

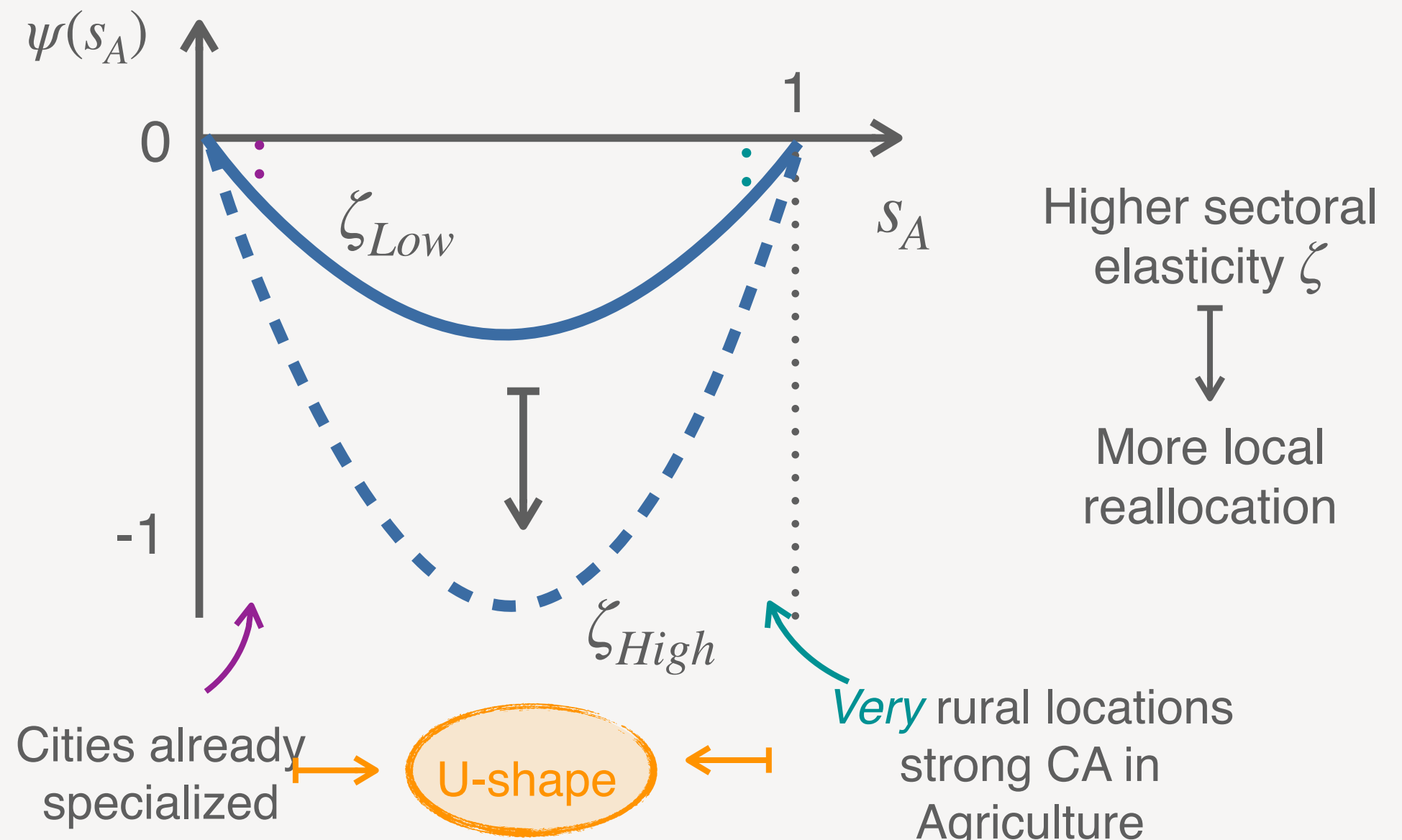
Spatially Biased Exposure: Wage Growth

$$d \ln \bar{w}_{rt} = \phi(s_{rA}) d \ln \mathcal{F}_{rMt} + \left(1 - \phi(s_{rA})\right) d \ln \mathcal{F}_{rAt}$$



Spatially Biased Exposure: Industrialization

$$ds_{rAt} = \psi(s_{rA}) (d \ln \mathcal{L}_{rMt} - d \ln \mathcal{L}_{rAt})$$



Can heterogeneity in exposure be enough?

- Suppose effective productivity growth was common [$\lambda_s = 0$, $\tau = 1$, No mobility]

$$d \ln \mathcal{F}_{rst} \equiv l_s$$

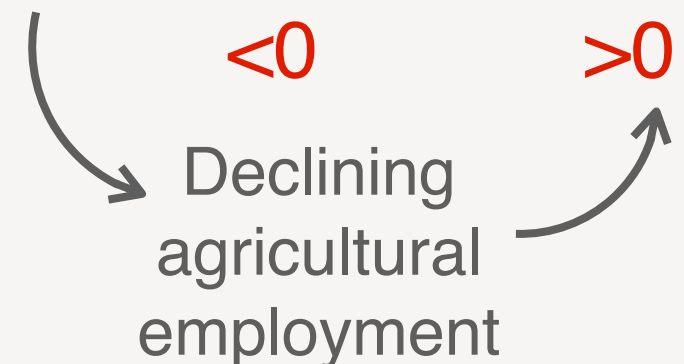
- Local growth:

$$d \ln \bar{w}_{rt} = d \ln l_A + \phi(s_{rA}) (d \ln l_M - d \ln l_A)$$

>0

$$\phi'(s_A) < 0 \longrightarrow \text{Urban bias!}$$

$$ds_{rAt} = \psi(s_{rA}) (d \ln l_M - d \ln l_A)$$



Rural bias $\longrightarrow \mathcal{F}_{rst}$ must have grown faster in rural America!

Today

- Theory
- Mechanism
- Estimation / Calibration
- Quantification: Importance of Rural Catch-Up

Data

- Panel of 503 commuting zones for 1880, 1900, 1920
 - Agricultural Employment Shares (*Decennial Census*)
 - Total Employment (*Decennial Census*)
 - Average Earnings in Manufacturing (*Census of Manufacturing*)
 - Average Value of Acre of Farm Land (*Census of Agriculture*)
- “Historical Statistics of the United States”
 - Time Series Data on GDP per capita, relative sectoral prices

Estimation Strategy

- Model inversion / Accounting:

$$\{Z_{rM1880}, Z_{rA1880}, T_{r1880}, B_{r1880}\}_r$$

- Time-Series estimation (“Macro”): $\{\eta, \nu, \phi\}, \{g_M, g_A\}$

- Indirect inference: $\{\lambda_M, \lambda_A, \zeta\}$

$$d \ln \bar{w}_{rt} = \delta_t + \beta_w s_{rAt} + \nu_{rt}$$

$$ds_{rAt} = \delta_t + \beta_{s_A} s_{rAt} + \gamma_{s_A} s_{rAt}^2 + u_{rt}$$

- Other targets: $\{\mu, \tau, \varepsilon\}$

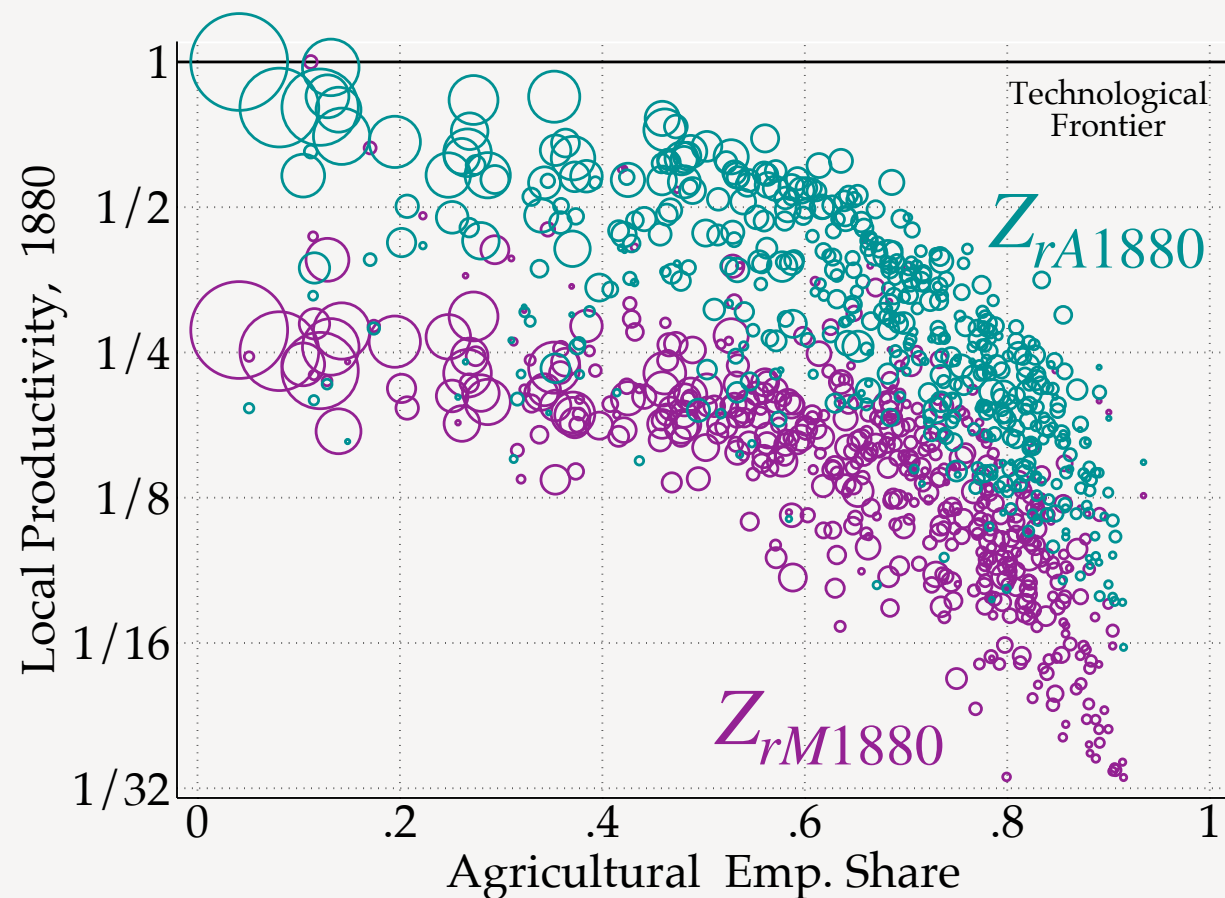
- Exogenous: $\{\alpha, \sigma\}$

Parameters

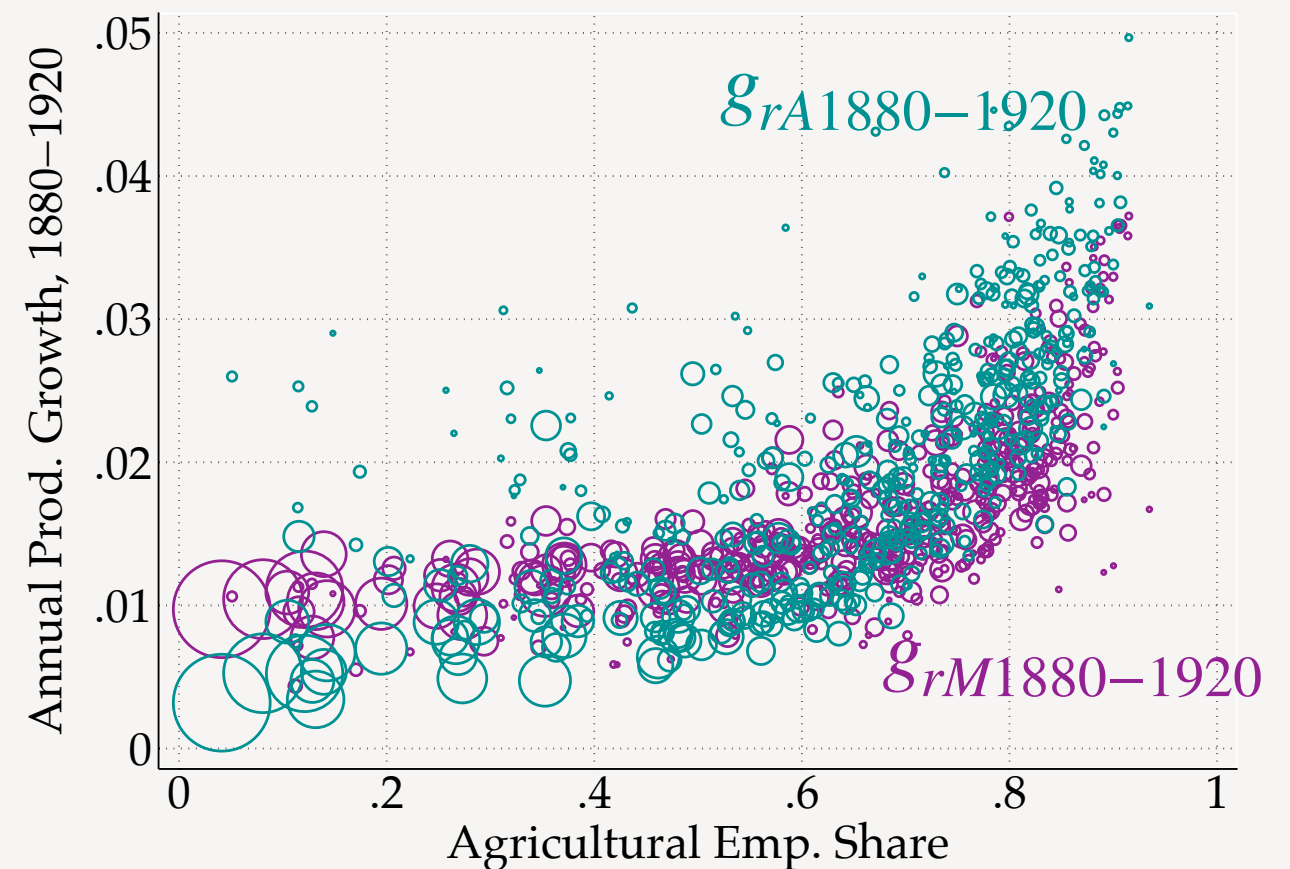
Moments

Rural Catch-Up: Estimates

The Productivity Ladder in 1880



The Rural Growth Premium

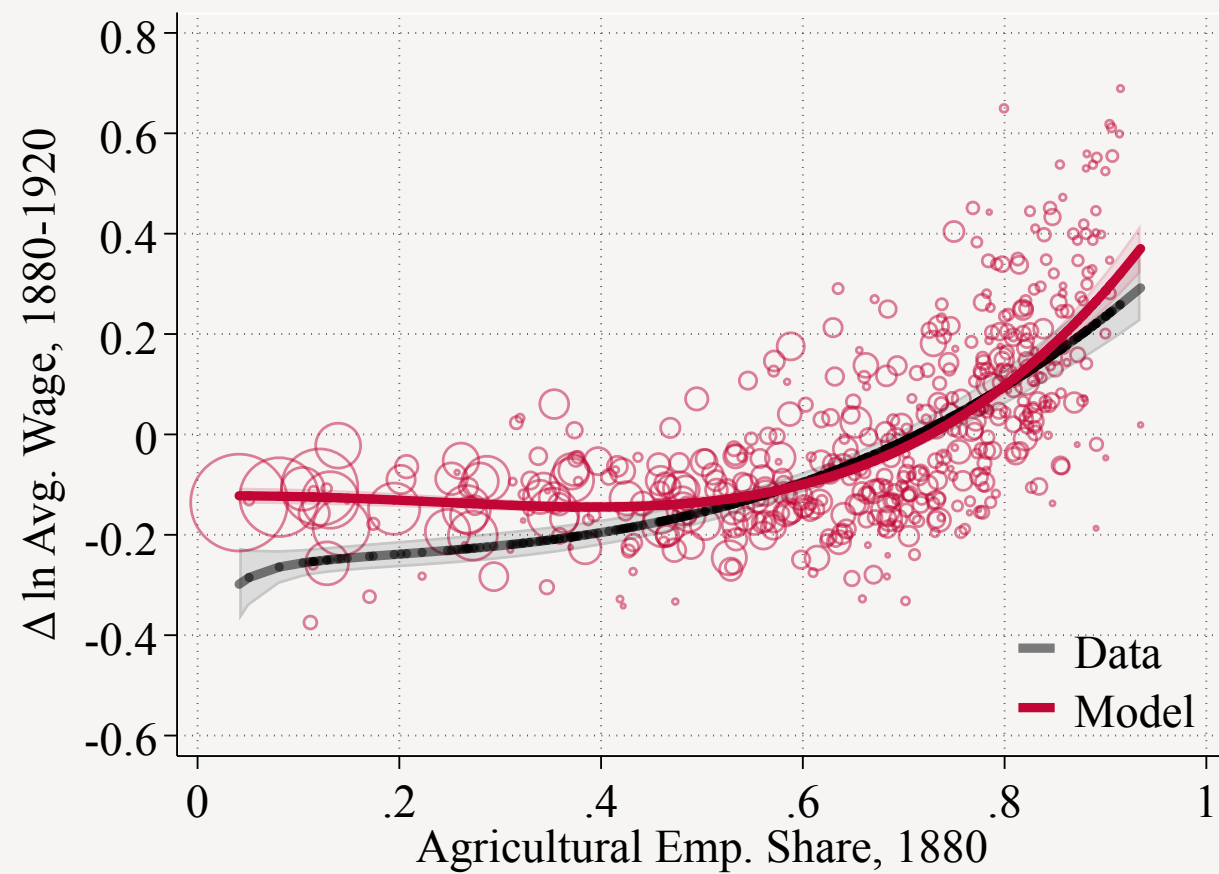


- Paper: Direct evidence for rural catch-up
 - Educational attainment, Financial developments, Capital deepening

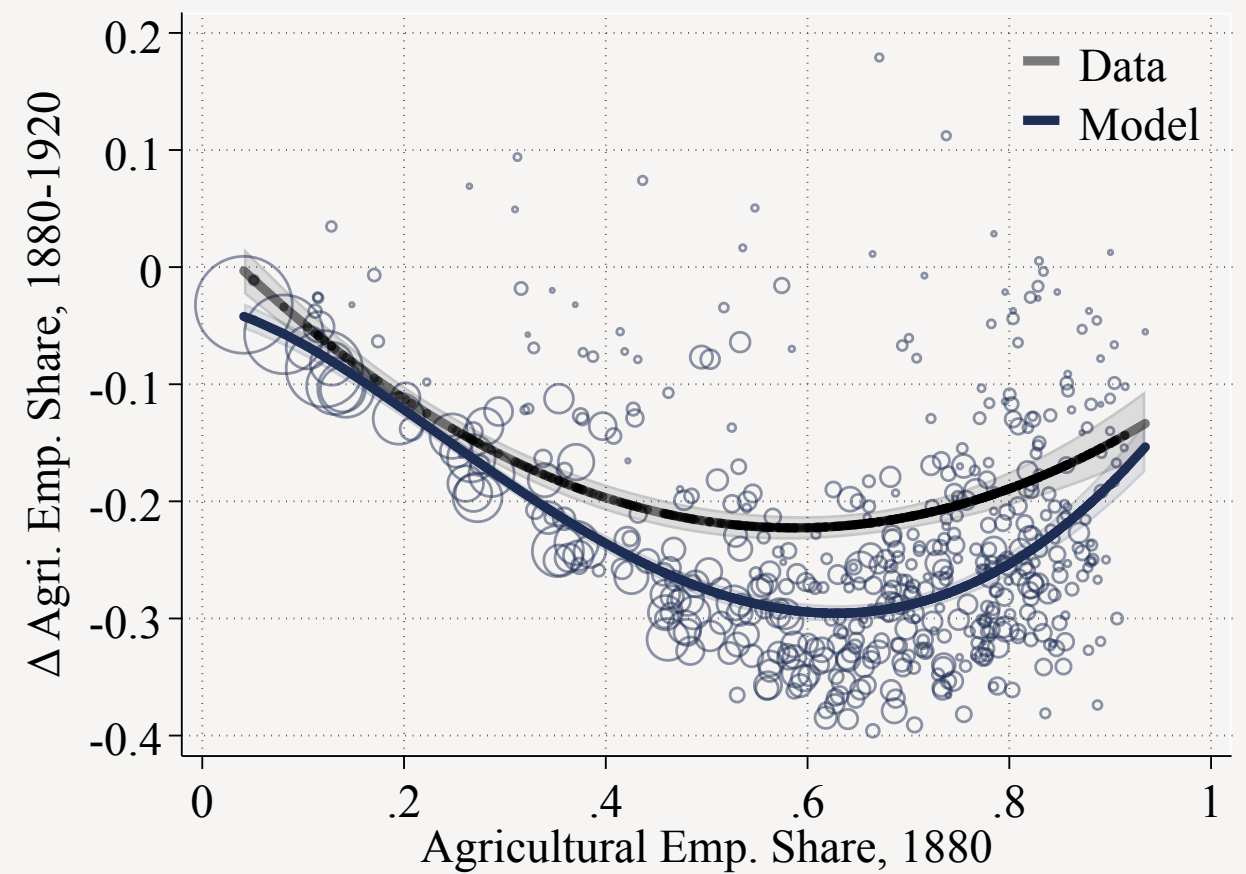
[Details](#)

Model Fit

Rural Wage Growth



Rural Industrialization



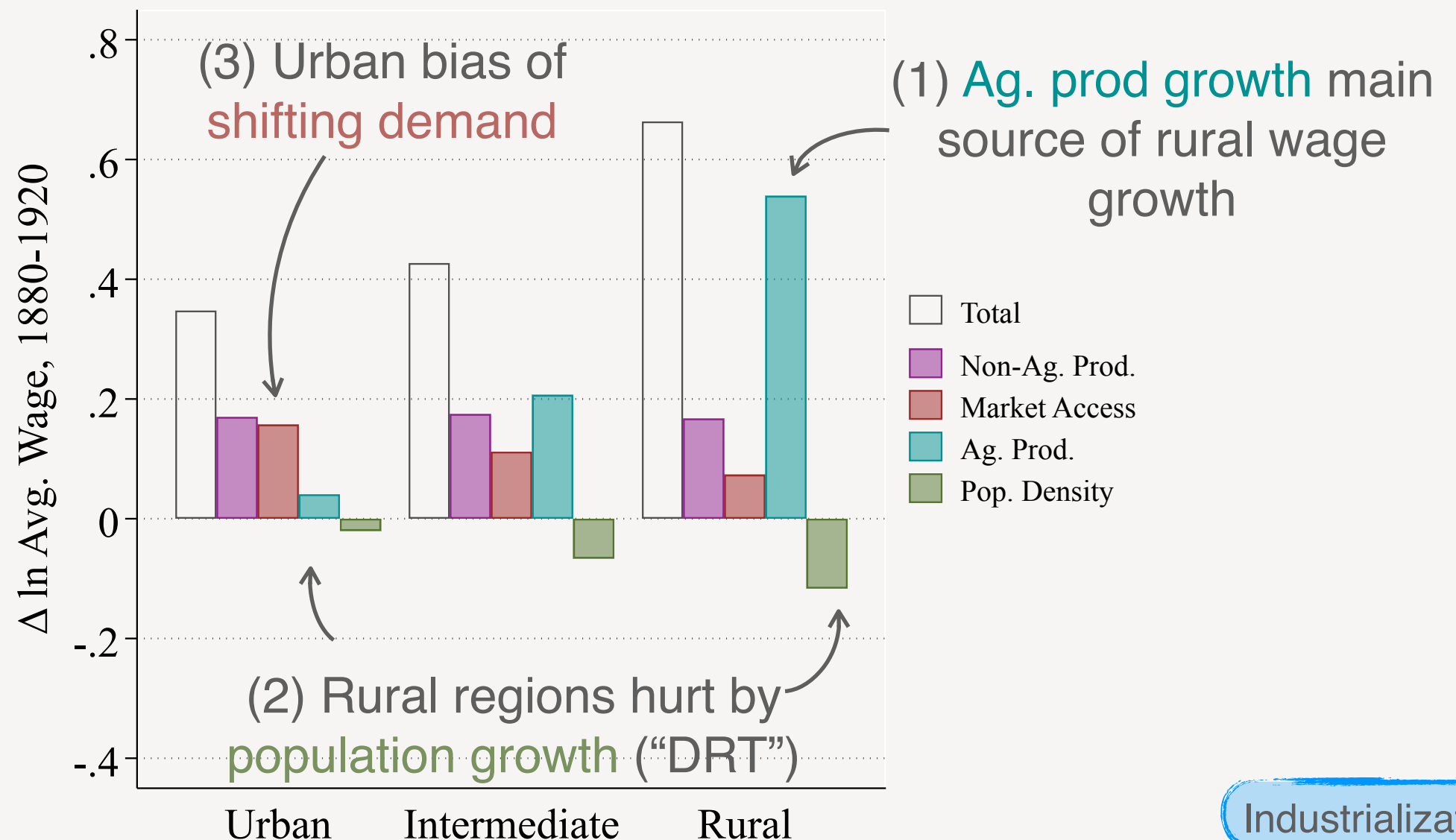
Population Growth

Today

- Theory
- Mechanism
- Estimation / Calibration
- Quantification: Importance of Rural Catch-Up

The Sources of Rural-Biased Growth

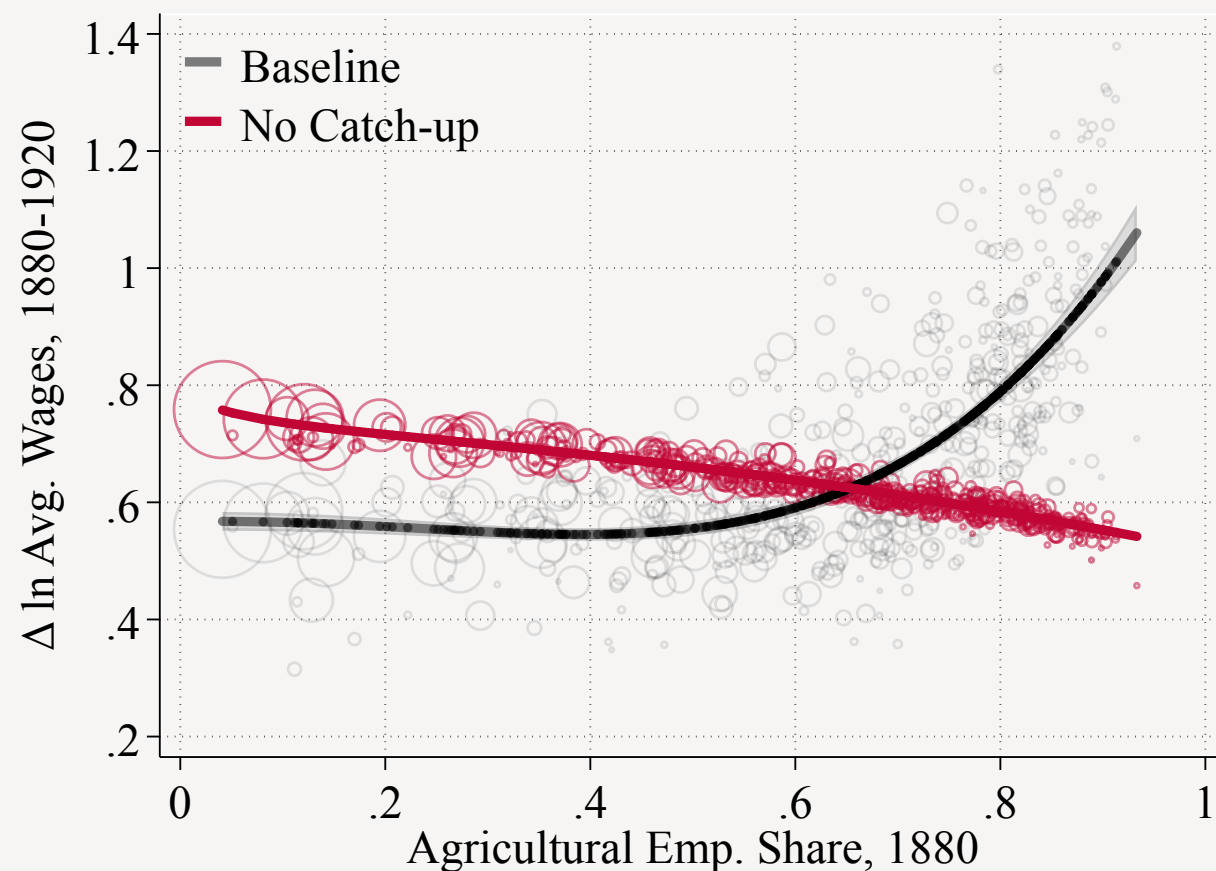
$$d \ln \bar{w}_{rt} = \phi(s_{rA}) \times \left(\underbrace{\frac{\sigma-1}{\sigma} d \ln Z_{rMt}}_{\text{Non-Ag. Prod.}} + \underbrace{\frac{1}{\sigma} d \ln \mathcal{D}_{rt}}_{\text{Demand}} \right) + \left(1 - \phi(s_{rA}) \right) \times \left(\underbrace{d \ln Z_{rAt}}_{\text{Ag. Prod.}} - \alpha \underbrace{d \ln \ell_{rt}}_{\text{Pop. density}} \right)$$



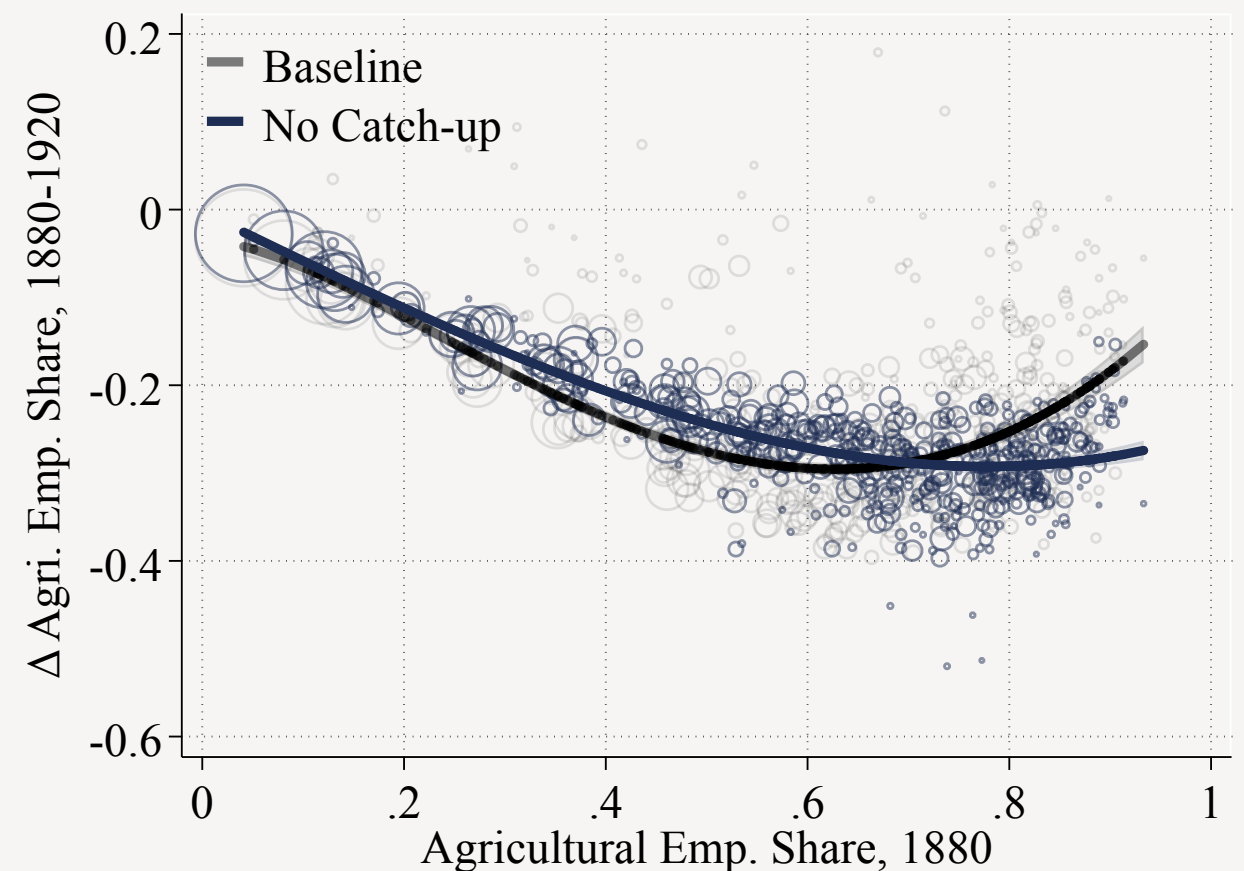
Industrialization

The Importance of Rural Catch-up

- Counterfactual “No-catch macro” calibration
 - Set $\lambda_M = \lambda_A = 0$
 - Recalibrate frontier growth g_M and g_A to match time-series moments



Urban biased growth



No U-shape

Convergence

Conclusion

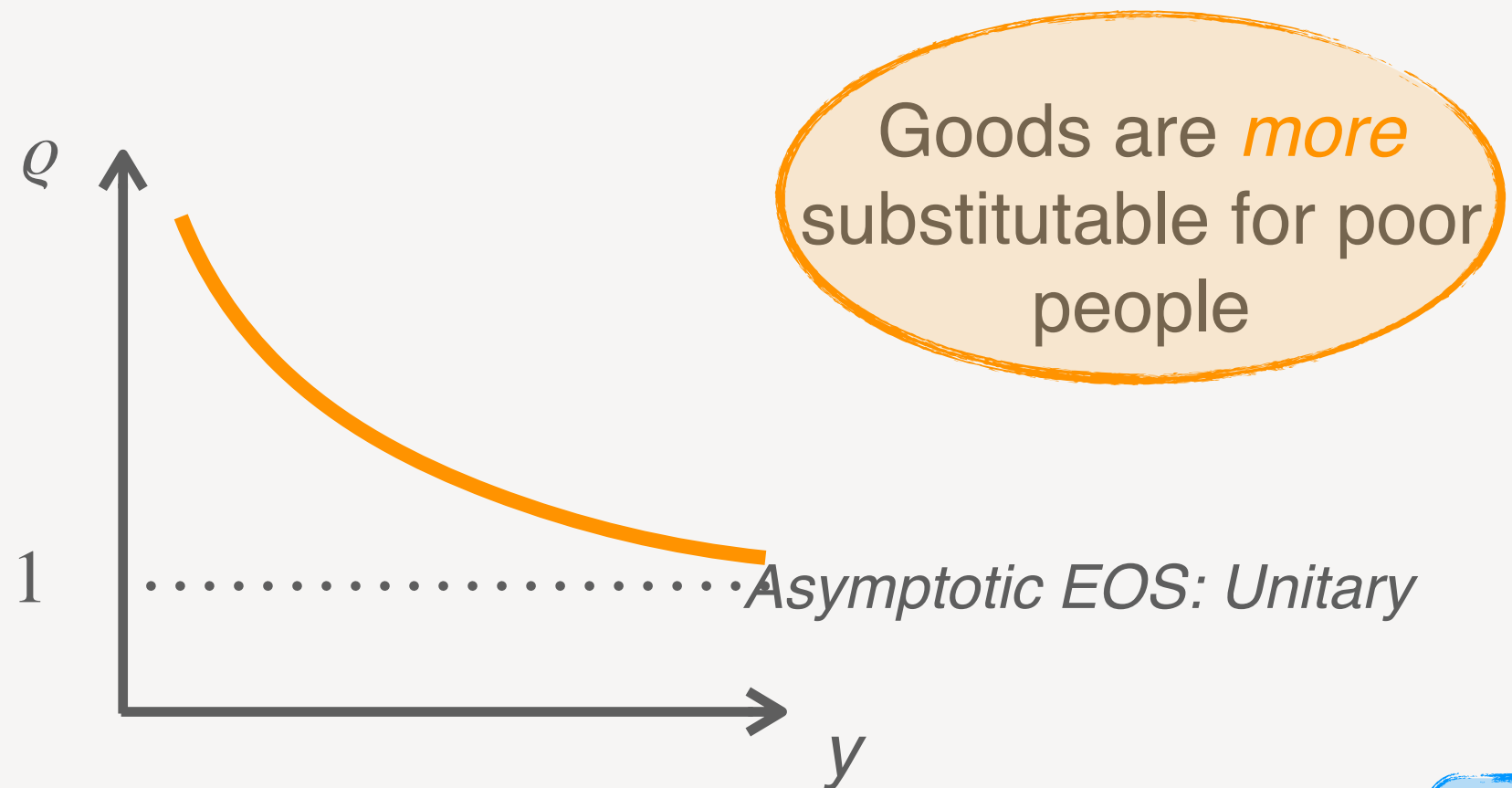
- US growth 1880-1920: Rural-biased
 - Faster wage growth & industrialization in rural areas
 - Spatial convergence
- Mechanism: Catch-up growth
 - Rural locations: at the bottom of the ladder in 1880
 - Catch-up growth = new opportunities to industrialize
- Looking ahead: Transition to services
 - Spatial divergence, not convergence
 - Service productivity = human capital; rival across space?

Appendix

Elasticity of Substitution

- The elasticity of substitution is given by

$$\varrho = 1 + \eta \frac{(\vartheta_A - \phi)^2}{\vartheta_A (1 - \vartheta_A)}$$



back

Aggregation: PIGL meets Frechet

With PIGL: analytical expression for aggregate demand and indirect utility

$$\frac{\int \vartheta_A(y, p_r) y dF_r(y)}{\int y dF_r(y)} = \phi + \nu^{\text{RC}} \left(\bar{w}_r / P_{rM}^{1-\phi} \right)^{-\eta} \quad \text{where}$$

$$\nu^{\text{RC}} \equiv \nu \frac{\Gamma_{\zeta/(1-\eta)}}{\Gamma_{\zeta}}$$

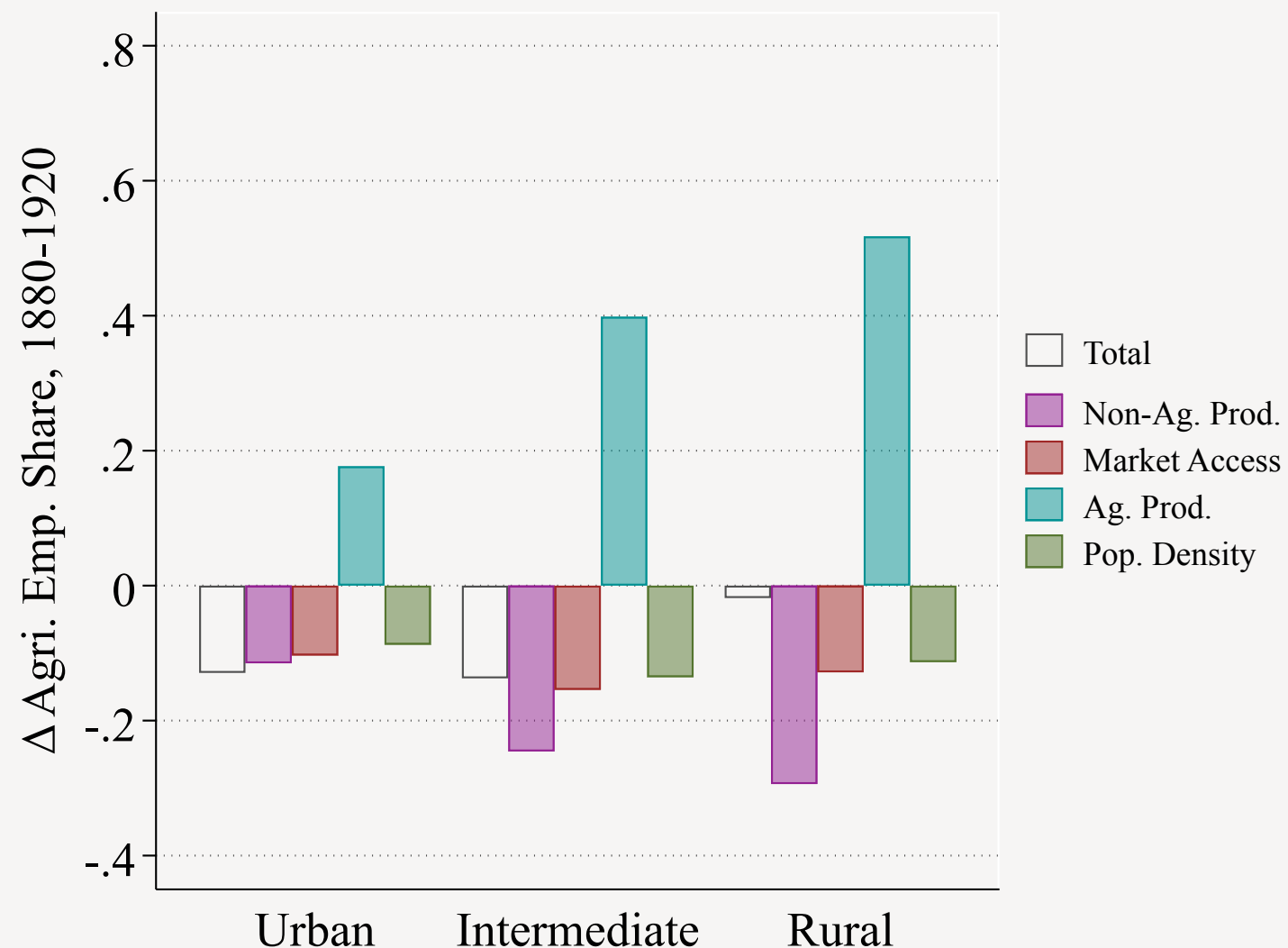
$$\text{Indirect utility:}$$

$$\mathcal{V}_r = \int V(y, p_r) dF_r(y) = \frac{1}{\eta} \Gamma_{\frac{\zeta}{\eta}} \left(\bar{w}_r / P_{rM}^{1-\phi} \right)^{\eta} - \nu \ln(1/P_{rM})$$

back

The Sources of Rural Industrialization

$$ds_{rAt} = \psi(s_{rA}) \times \left(\underbrace{\frac{\sigma - 1}{\sigma} d \ln Z_{rMt}}_{\text{Non-Ag. Prod.}} + \underbrace{\frac{1}{\sigma} d \ln \mathcal{D}_{rt}}_{\text{Demand}} - \left(\underbrace{d \ln Z_{rAt}}_{\text{Ag. Prod.}} - \alpha \underbrace{d \ln \ell_{rt}}_{\text{Pop. density}} \right) \right)$$



back

Rural Catch-up: Empirical Evidence

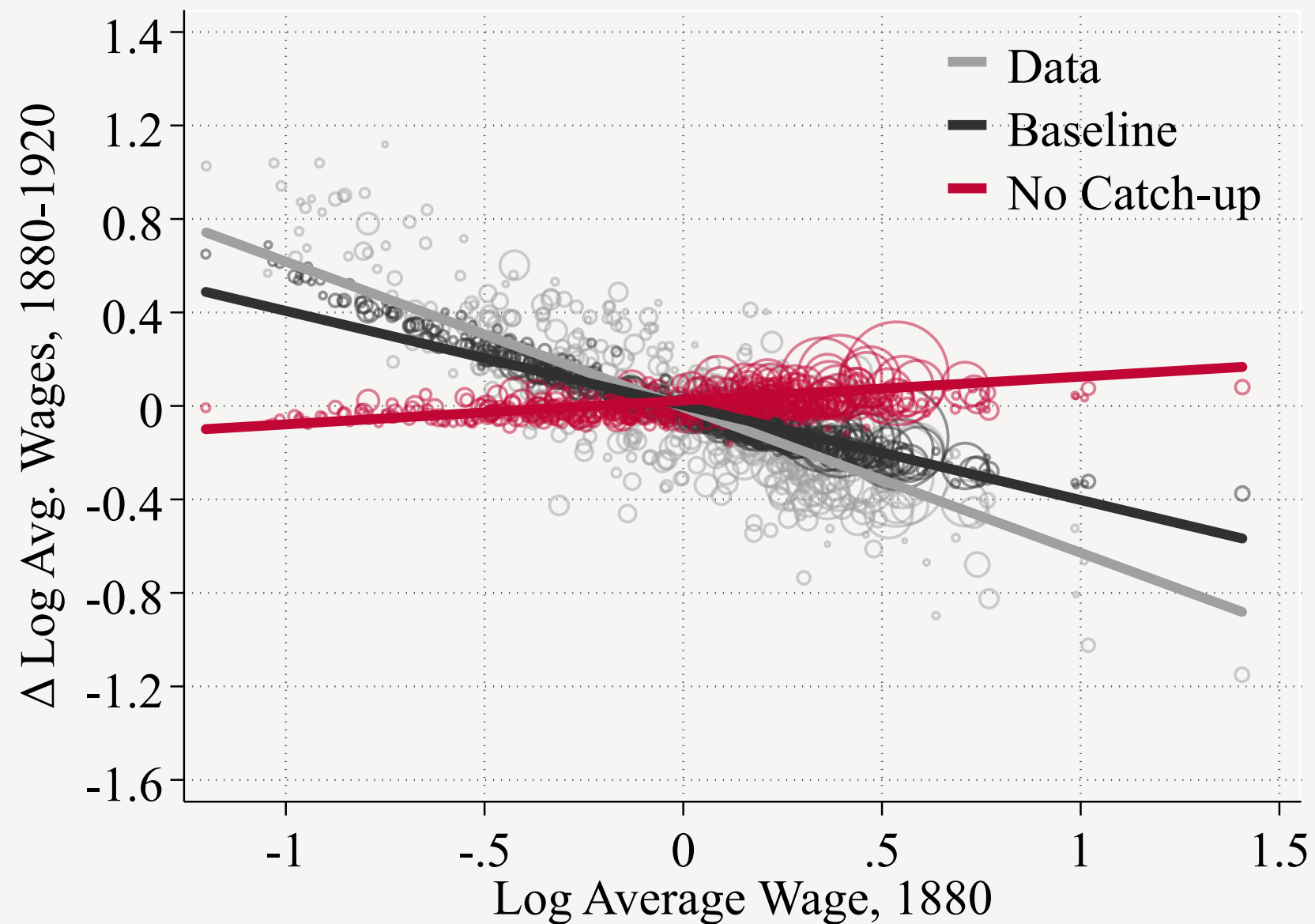
TABLE 2: DRIVERS OF RURAL CATCH-UP

	GROWTH IN...					
	GENERAL		SECTOR-SPECIFIC FACTORS			
	Banks pc	School Atten- dance	Agri. Machi- nery	Farm Size	Non-agri. Machi- nery	Plant Size
Agri. Emp. Share	0.117*** (0.006)	0.007*** (0.001)	0.032*** (0.002)	0.012*** (0.003)	0.039*** (0.009)	0.032*** (0.007)
R^2	0.723	0.331	0.359	0.107	0.090	0.242
N	495	495	495	495	495	495

Notes: The dependent variables are the growth rate in the number of banks per capita from [Jaremski and Fishback \[2018\]](#) (Column 1), the change in the share of children attending school from the Decennial Census (Column 2), and the growth rates of the sectoral capital stocks and average employment per farm/firm from the Census of Manufacturing (Columns 5 and 6) and the Census of Agriculture (Columns 3 and 4). All regressions are employment weighted.

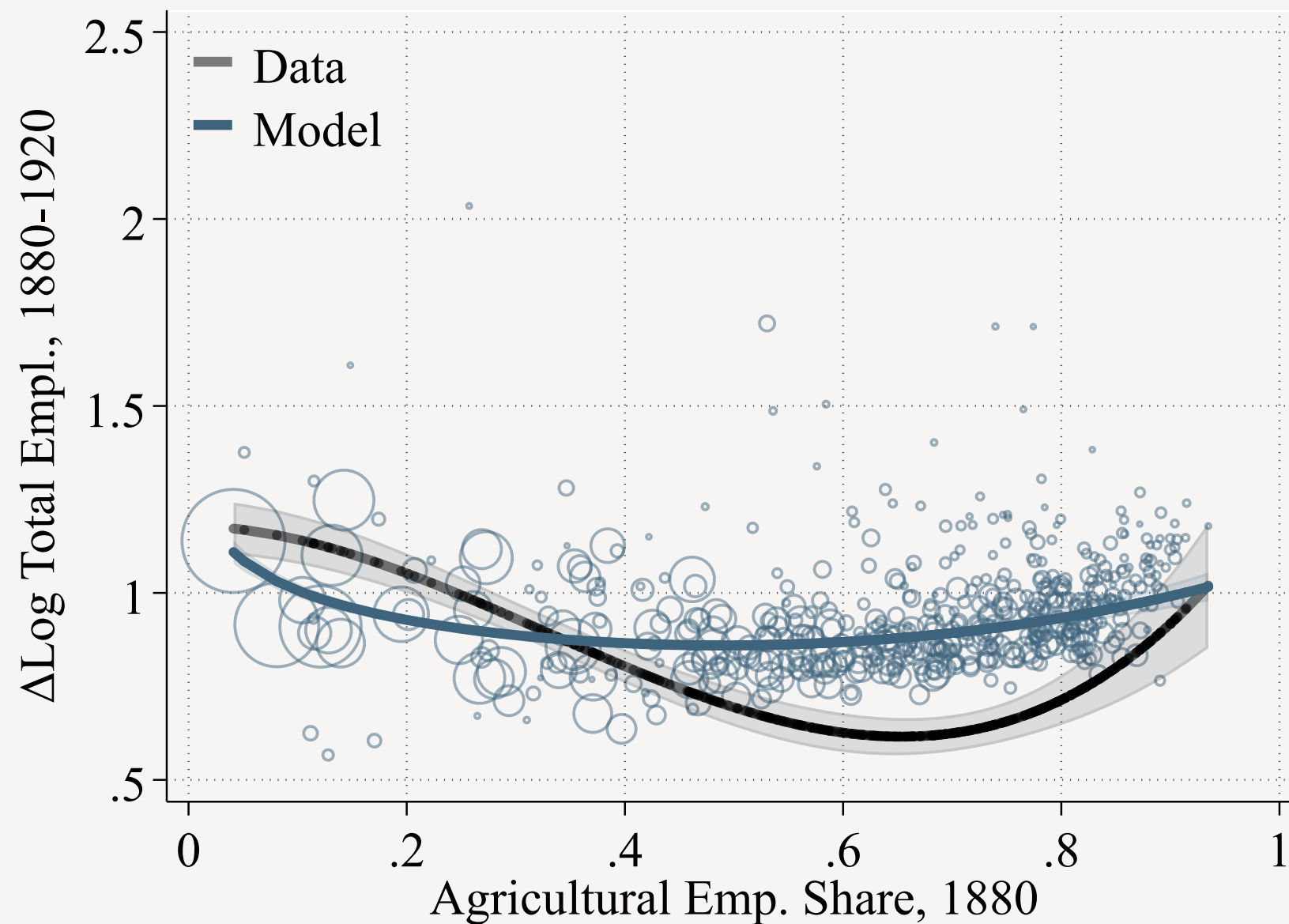
back

Catch-up and Convergence



[back](#)

Model Fit: Population Growth



[back](#)

Estimated Parameters & Moments

STRUCTURAL PARAMETERS			ESTIMATION METHOD		
	DESCRIPTION	VALUE	PANEL A: IN-MODEL (MOMENT, DATA, MODEL)		
ζ	Labor Supply Elasticity	6.9	γ_{sA} in regression (17)	0.45	0.51
			$E[s_{rA1920} - s_{rA1880} s_{rA1880} > 0.8]$	-0.20	-0.20
λ_A	Catch-Up in Agricult.	0.21	β_w in regression (17)	0.25	0.16
g_A	Growth of Agricult. Frontier	0.07	Ag. Empl. Share 1900	0.39	0.35
		0.12	Ag. Empl. Share 1920	0.26	0.25
λ_M	Catch-Up in Non-agricult.	0.05	β_{sA} in regression (17)	-0.48	-0.57
g_M	Growth of Non-agricult. Frontier	0.09	GDP growth 1880-1900	1.43	1.50
			GDP growth 1900-1920	2.04	2.05
ϵ	Location Taste Heterogeneity	3.80	Avg. Migration Elasticity	2	2.03
			β_l in regression (19)	-0.36	-0.04
η	Engel Elasticity	0.93	Rel. price P_M/P_A 1900	0.94	1.01
ν	PIGL preference parameter	0.12	Rel. price P_M/P_A 1920	0.89	0.87
			PANEL B: OUT-OF-MODEL (STRATEGY)		
κ	Migration Cost Distance Elasticity	2.8	Gravity relationship of migration flows		
θ	Trade Costs Distance Elasticity	1.35	Gravity relationship of trade flows		
			PANEL C: EXOGENOUSLY-SET (SOURCE)		
σ	Elasticity of Substitution Mfg Good	6	NA		
ρ	Amenity Congestion Elasticity	0.15	Allen and Donaldson [2020]		
α	Land Share in Production Function	0.4	Valentinyi and Herrendorf [2008]		
ϕ	Asy. Exp. Share on Agricult. Goods	0.01	NA		

[back](#)